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Parallel Programming in C with MPI and OpenMP

Michael J. Quinn



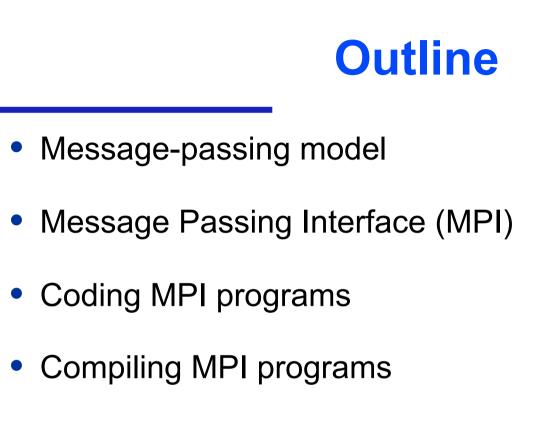
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Chapter 4

Message-Passing Programming

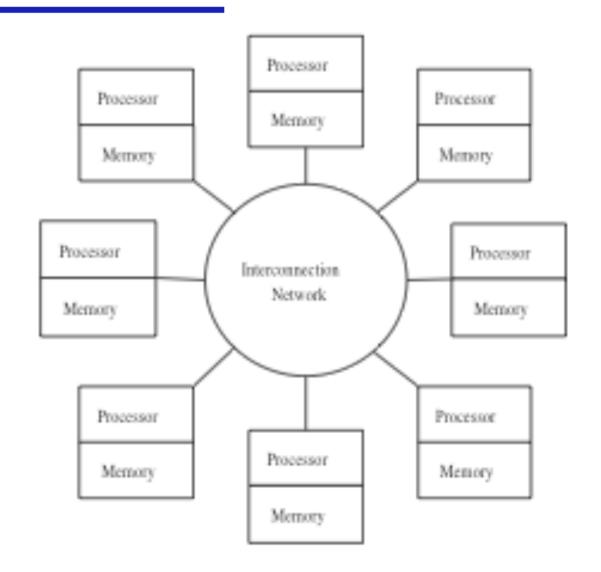
Learning Objectives

- Understanding how MPI programs execute
- Familiarity with fundamental MPI functions



- Running MPI programs
- Benchmarking MPI programs

Message-passing Model



Processes

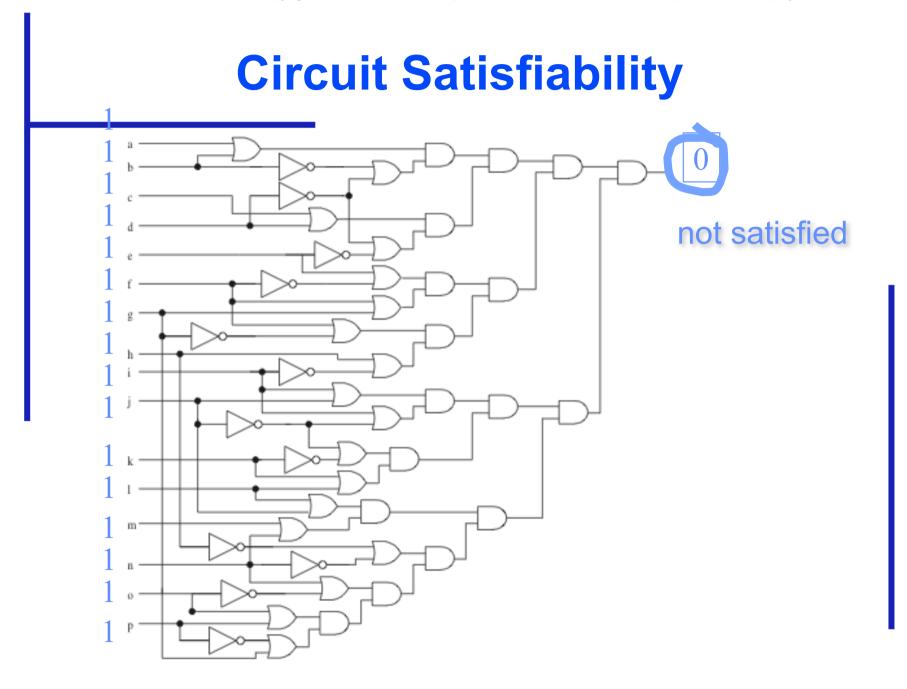
- Number is specified at start-up time
- Remains constant throughout execution of program
- All execute same program
- Each has unique ID number
- Alternately performs computations and communicates

Advantages of Message-passing Model

- Gives programmer ability to manage the memory hierarchy
- Portability to many architectures
- Easier to create a deterministic program
- Simplifies debugging

The Message Passing Interface

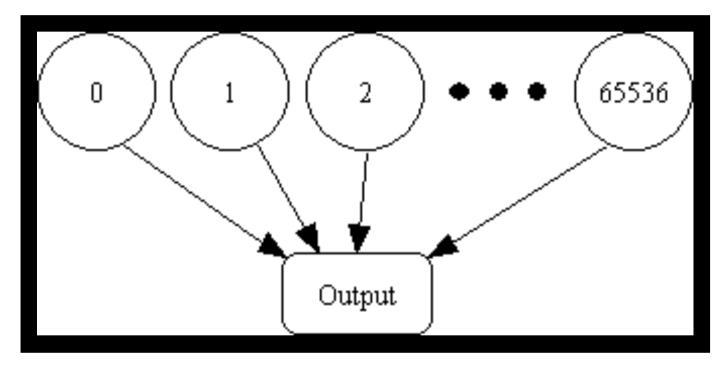
- Late 1980s: vendors had unique libraries
- 1989: Parallel Virtual Machine (PVM) developed at Oak Ridge National Lab
- 1992: Work on MPI standard begun
- 1994: Version 1.0 of MPI standard
- 1997: Version 2.0 of MPI standard
- Today: MPI is dominant message passing library standard



Solution Method

- Circuit satisfiability is NP-complete
- No known algorithms to solve in polynomial time
- We seek all solutions
- We find through exhaustive search
- 16 inputs \Rightarrow 65,536 combinations to test

Partitioning: Functional Decomposition



Embarrassingly parallel: No channels between tasks

Agglomeration and Mapping

- Properties of parallel algorithm
 - Fixed number of tasks
 - No communications between tasks
 - Time needed per task is variable
- Map tasks to processors in a cyclic fashion

Cyclic (interleaved) Allocation

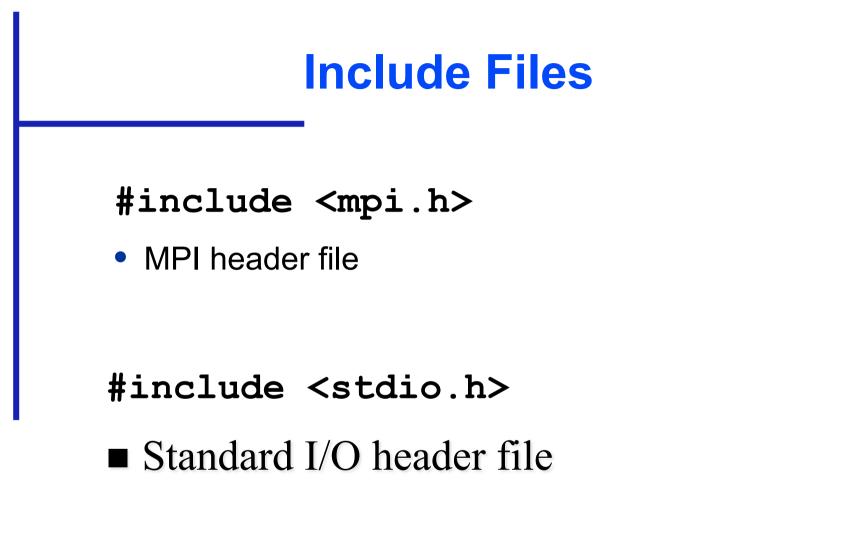
- Assume *p* processes
- Each process gets every p^{th} piece of work
- Example: 5 processes and 12 pieces of work
 - *P*₀: 0, 5, 10
 - *P*₁: 1, 6, 11
 - P₂: 2, 7
 - P₃: 3, 8
 - P₄: 4, 9



- Assume n pieces of work, p processes, and cyclic allocation
- What is the most pieces of work any process has?
- What is the least pieces of work any process has?
- How many processes have the most pieces of work?

Summary of Program Design

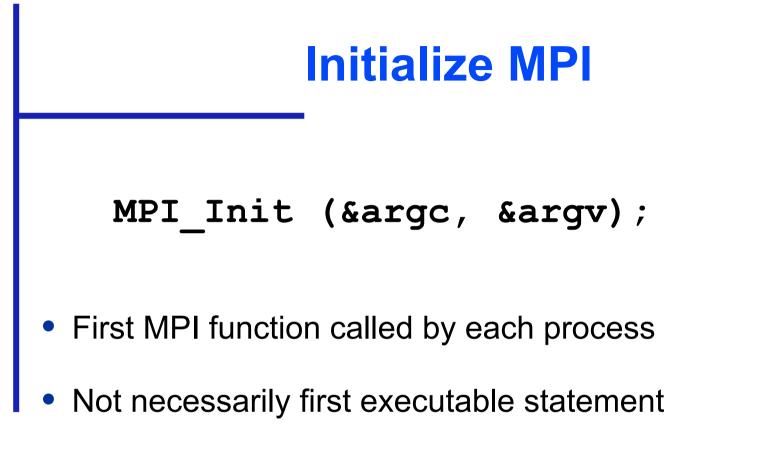
- Program will consider all 65,536 combinations of 16 boolean inputs
- Combinations allocated in cyclic fashion to processes
- Each process examines each of its combinations
- If it finds a satisfiable combination, it will print it



Local Variables

```
int main (int argc, char *argv[]) {
    int i;
    int id; /* Process rank */
    int p; /* Number of processes */
    void check_circuit (int, int);
```

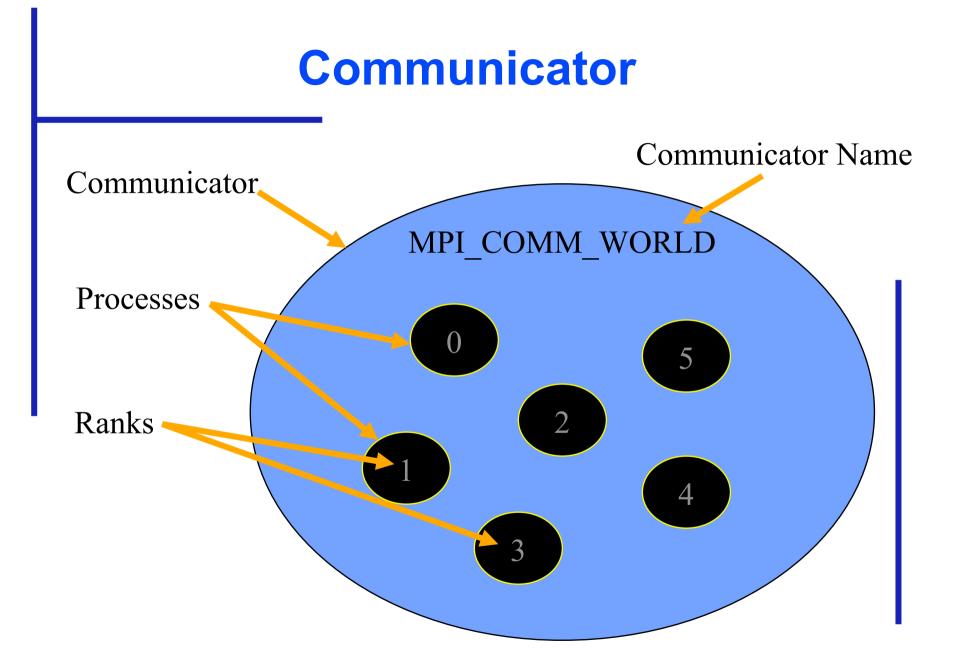
- Include argc and argv: they are needed to initialize MPI
- One copy of every variable for each process running this program

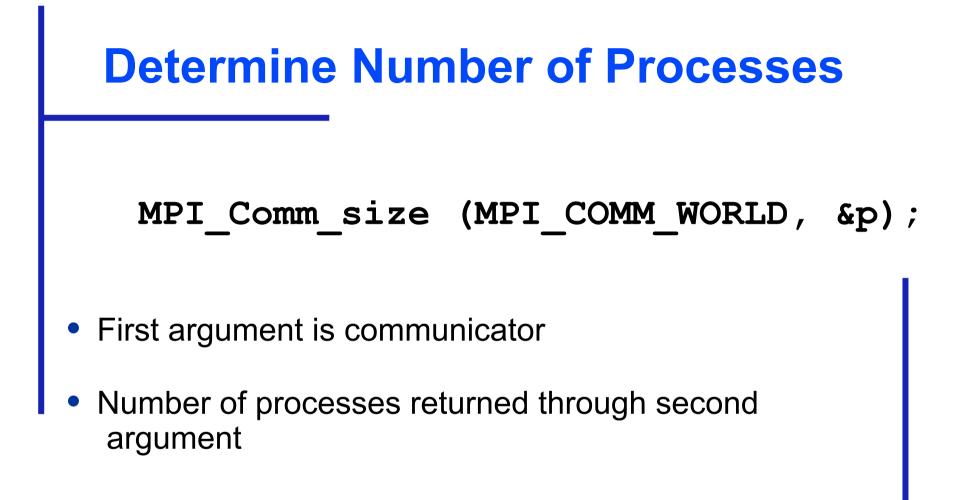


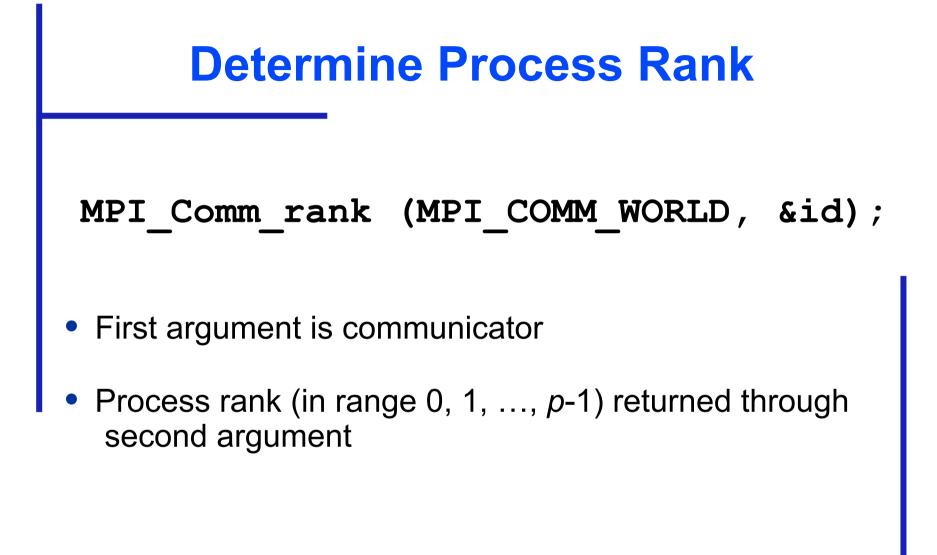
Allows system to do any necessary setup

Communicators

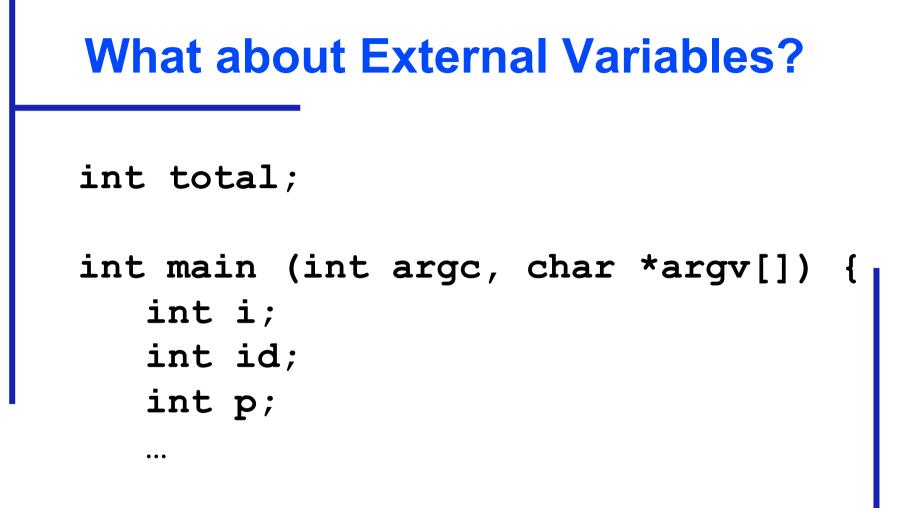
- Communicator: opaque object that provides message -passing environment for processes
- MPI_COMM_WORLD
 - Default communicator
 - Includes all processes
- Possible to create new communicators
 - Will do this in Chapters 8 and 9







Replication of Automatic Variables id 0 id 2 id 1 6 p 6 p 6 p id 3 id 5 id 4 6 p 6 p 6 p

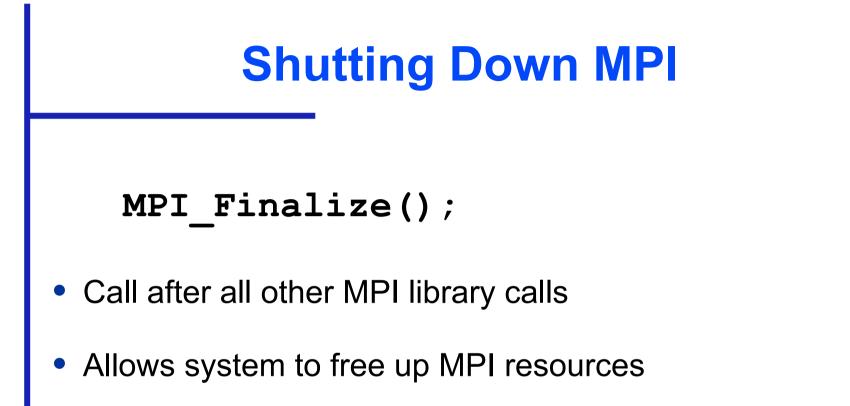


■ Where is variable total stored?



```
for (i = id; i < 65536; i += p)
    check_circuit (id, i);</pre>
```

- Parallelism is outside function
 check_circuit
- It can be an ordinary, sequential function

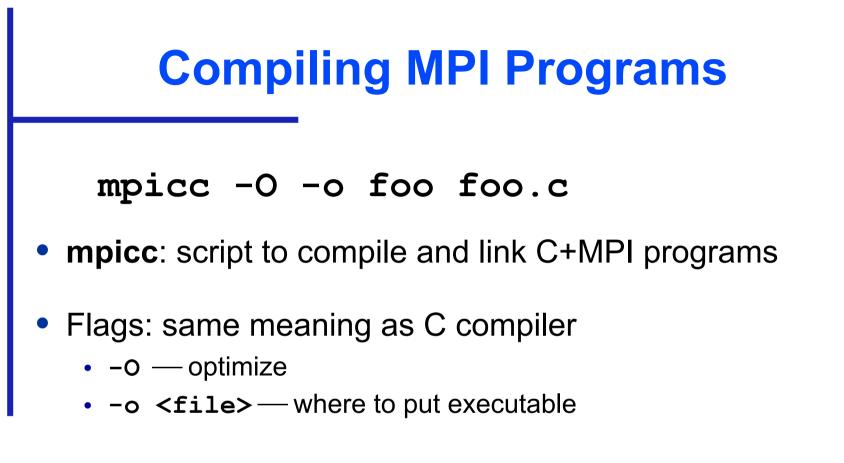


```
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```

```
#include <mpi.h>
#include <stdio.h>
int main (int argc, char *argv[]) {
   int i;
   int id;
   int p;
  void check circuit (int, int);
  MPI Init (&argc, &argv);
  MPI Comm rank (MPI COMM WORLD, &id);
  MPI Comm size (MPI COMM WORLD, &p);
   for (i = id; i < 65536; i += p)
      check circuit (id, i);
   printf ("Process %d is done\n", id);
  fflush (stdout);
  MPI Finalize();
   return 0;
            Put fflush() after every printf
}
```

```
/* Return 1 if 'i'th bit of 'n' is 1; 0 otherwise */
#define EXTRACT BIT(n,i) ((n&(1<<i))?1:0)</pre>
```

```
void check circuit (int id, int z) {
   int v[16]; /* Each element is a bit of z */
   int i;
   for (i = 0; i < 16; i++) v[i] = EXTRACT BIT(z,i);
   if ((v[0] || v[1]) \&\& (!v[1] || !v[3]) \&\& (v[2] || v[3])
     \&\& (!v[3] || !v[4]) && (v[4] || !v[5])
     \&\& (v[5] || !v[6]) && (v[5] || v[6])
     && (v[6] || !v[15]) \& (v[7] || !v[8])
     && (!v[7] || !v[13]) \&\& (v[8] || v[9])
     && (v[8] || !v[9]) \&\& (!v[9] || !v[10])
     && (v[9] || v[11]) && (v[10] || v[11])
     \&\& (v[12] || v[13]) \&\& (v[13] || !v[14])
     \&\& (v[14] | | v[15])) \{
     v[0],v[1],v[2],v[3],v[4],v[5],v[6],v[7],v[8],v[9],
        v[10],v[11],v[12],v[13],v[14],v[15]);
     fflush (stdout);
   }
}
```



Running MPI Programs

- mpirun -np <exec> <arg1> ...
 - -np number of processes
 - <exec> executable
 - <arg1> ... command-line arguments

Specifying Host Processors

- File .mpi-machines in home directory lists host processors in order of their use
- Example .mpi_machines file contents

band01.cs.ppu.edu band02.cs.ppu.edu

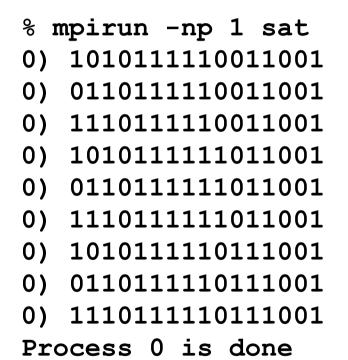
band03.cs.ppu.edu

band04.cs.ppu.edu

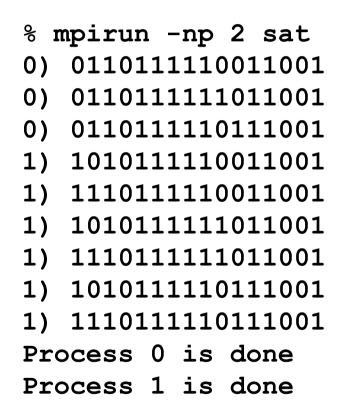
Enabling Remote Logins

- MPI needs to be able to initiate processes on other processors without supplying a password
- Each processor in group must list all other processors in its .rhosts file; e.g., band01.cs.ppu.edu student band02.cs.ppu.edu student band03.cs.ppu.edu student band04.cs.ppu.edu student

Execution on 1 CPU



Execution on 2 CPUs



Execution on 3 CPUs

% n	npirur	า -	-np	3	sat
0)	01101	11	L11(01	1001
0)	11101	11	L111	L01	1001
2)	10101	11	L11(001	1001
1)	11101	11	L11(001	1001
1)	10101	11	L111	L01	1001
1)	01101	11	L11()11	1001
0)	10101	11	L11()11	1001
2)	01101	11	L111	L01	1001
2)	11101	11	L11()11	1001
Pro	cess	1	is	dc	one
Pro	cess	2	is	dc	ne
Pro	cess	0	is	dc	ne

Deciphering Output

- Output order only partially reflects order of output events inside parallel computer
- If process A prints two messages, first message will appear before second
- If process A calls printf before process B, there is no guarantee process A's message will appear before process B's message

Enhancing the Program

- We want to find total number of solutions
- Incorporate sum-reduction into program
- Reduction is a collective communication



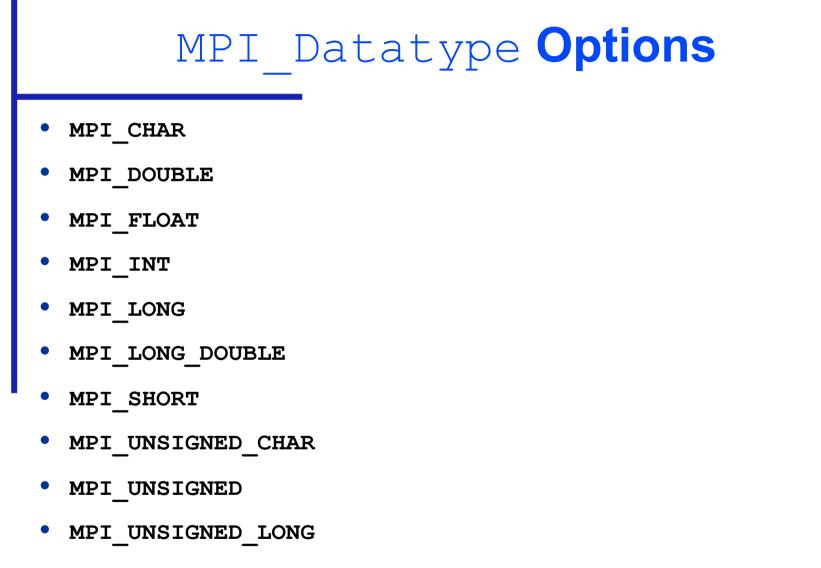
- Modify function check_circuit
 - Return 1 if circuit satisfiable with input combination
 - Return 0 otherwise
- Each process keeps local count of satisfiable circuits it has found
- Perform reduction after for loop

New Declarations and Code

```
int count; /* Local sum */
int global_count; /* Global sum */
int check_circuit (int, int);
```

```
count = 0;
for (i = id; i < 65536; i += p)
     count += check_circuit (id, i);
```

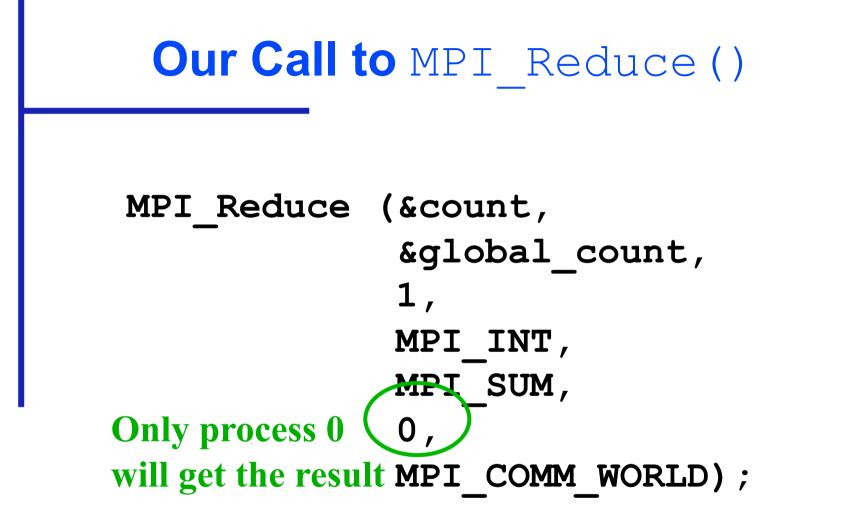
Prototype of MPI_Reduce()



MPI_UNSIGNED_SHORT

MPI_Op Options

- MPI_BAND
- MPI_BOR
- MPI_BXOR
- MPI_LAND
- MPI_LOR
- MPI_LXOR
- MPI_MAX
- MPI_MAXLOC
- MPI_MIN
- MPI_MINLOC
- MPI_PROD
- MPI_SUM



if (!id) printf ("There are %d different solutions\n",
 global_count);

Execution of Second Program

% mpirun -np 3 seq2 0) 0110111110011001 0) 1110111111011001 1) 1110111110011001 1) 1010111111011001 2) 1010111110011001 2) 0110111111011001 2) 1110111110111001 1) 0110111110111001 0) 1010111110111001 Process 1 is done Process 2 is done Process 0 is done There are 9 different solutions

Benchmarking the Program

- MPI Barrier barrier synchronization
- MPI_Wtick timer resolution
- MPI Wtime current time

Benchmarking Code

```
double elapsed time;
```

...

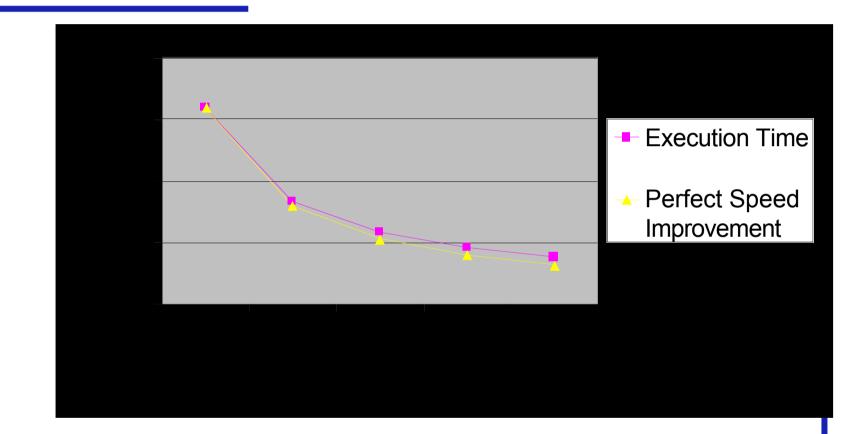
```
MPI_Init (&argc, &argv);
MPI_Barrier (MPI_COMM_WORLD);
elapsed_time = - MPI_Wtime();
...
MPI_Reduce (...);
```

```
elapsed_time += MPI_Wtime();
```

Benchmarking Results

Processors	Time (sec)
1	15.93
2	8.38
3	5.86
4	4.60
5	3.77

Benchmarking Results





- Message-passing programming follows naturally from task/channel model
- Portability of message-passing programs
- MPI most widely adopted standard

Summary (2/2)

- MPI functions introduced
 - MPI_Init
 - MPI_Comm_rank
 - MPI_Comm_size
 - MPI_Reduce
 - MPI_Finalize
 - MPI_Barrier
 - MPI_Wtime
 - MPI_Wtick

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Chapter 6

Floyd's Algorithm

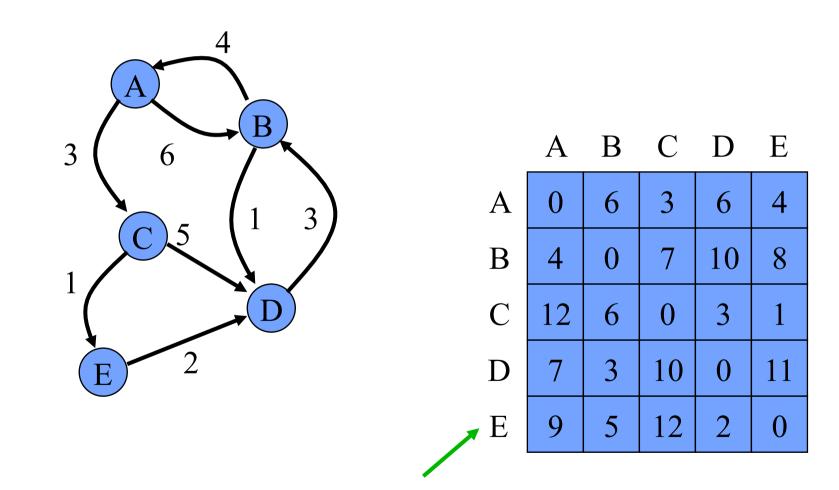
Chapter Objectives

- Creating 2-D arrays
- Thinking about "grain size"
- Introducing point-to-point communications
- Reading and printing 2-D matrices
- Analyzing performance when computations and communications overlap



- All-pairs shortest path problem
- Dynamic 2-D arrays
- Parallel algorithm design
- Point-to-point communication
- Block row matrix I/O
- Analysis and benchmarking

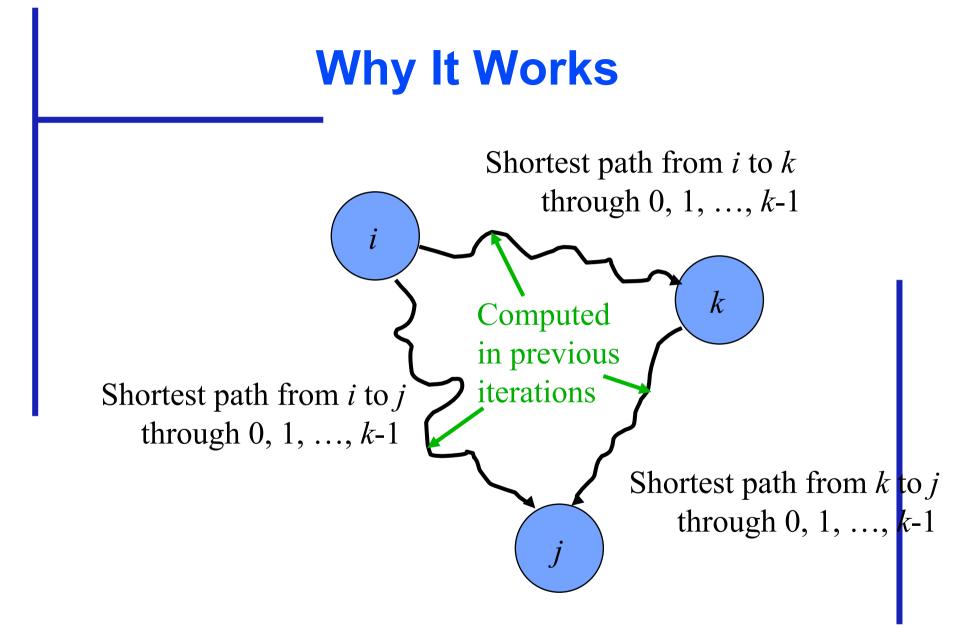
All-pairs Shortest Path Problem



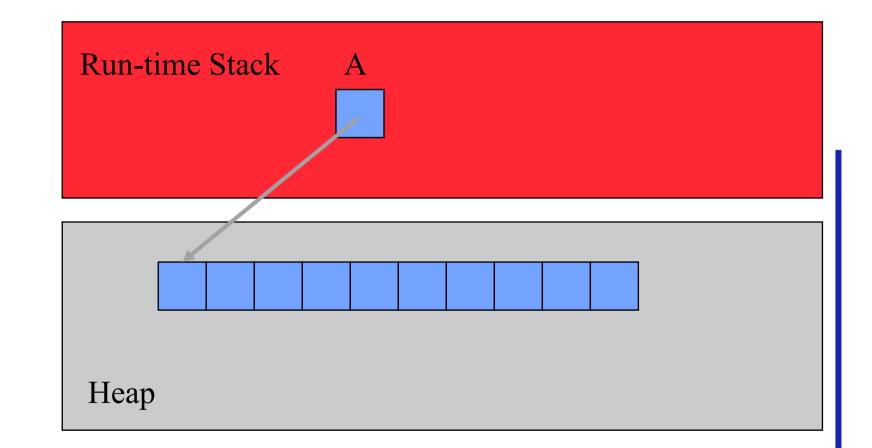
Resulting Adjacency Matrix Containing Distances



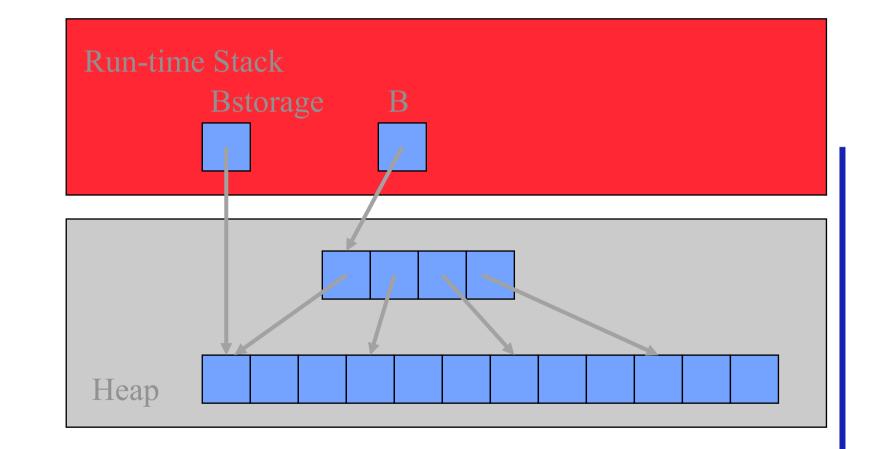
```
for k \leftarrow 0 to n-1
for i \leftarrow 0 to n-1
for j \leftarrow 0 to n-1
a[i,j] \leftarrow \min(a[i,j], a[i,k] + a[k,j])
endfor
endfor
endfor
```



Dynamic 1-D Array Creation



Dynamic 2-D Array Creation

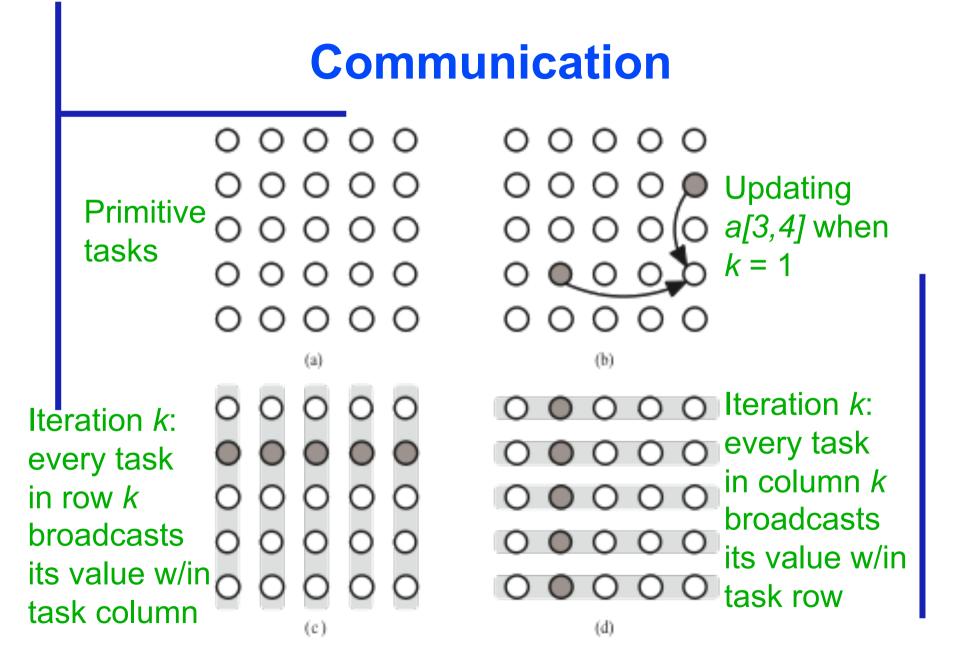


Designing Parallel Algorithm

- Partitioning
- Communication
- Agglomeration and Mapping

Partitioning

- Domain or functional decomposition?
- Look at pseudocode
- Same assignment statement executed *n*³ times
- No functional parallelism
- Domain decomposition: divide matrix A into its n² elements



Agglomeration and Mapping

- Number of tasks: static
- Communication among tasks: structured
- Computation time per task: constant
- Strategy:
 - Agglomerate tasks to minimize communication
 - Create one task per MPI process





Columnwise block striped

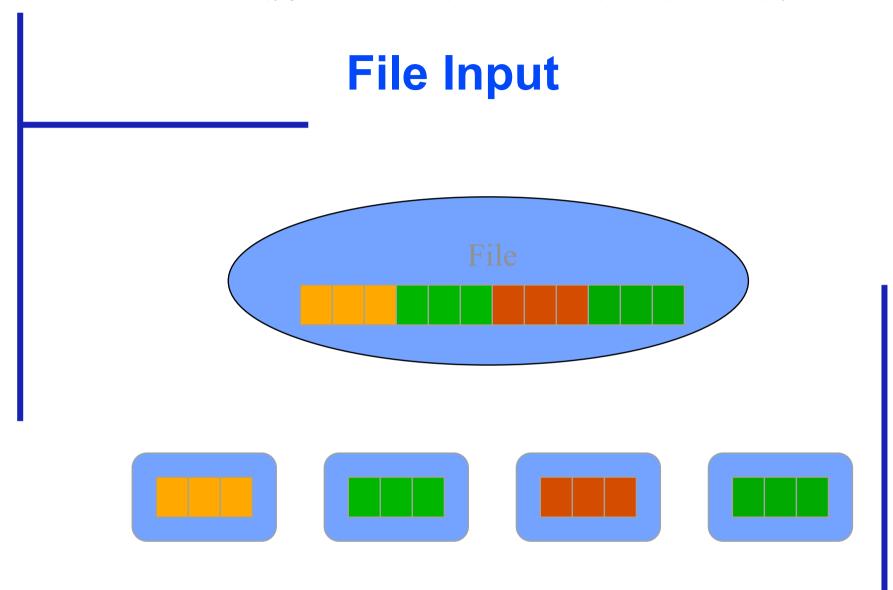
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(b)

Comparing Decompositions

- Columnwise block striped
 - Broadcast within columns eliminated
- Rowwise block striped
 - Broadcast within rows eliminated
 - Reading matrix from file simpler
- Choose rowwise block striped decomposition

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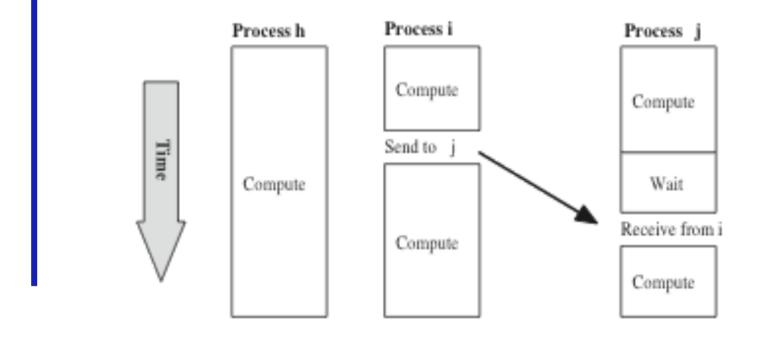


Why don't we input the entire file at once and then scatter its contents among the processes, allowing concurrent message passing?

Point-to-point Communication

- Involves a pair of processes
- One process sends a message
- Other process receives the message

Send/Receive Not Collective



Function MPI_Send

int MPI Send (

void	*message,
void	*message

int dest,

int tag,

MPI Comm

comm

Function MPI_Recv							
int MPI_Recv (
void	*message,						
int	count,						
MPI_Datatype	datatype,						
int	source,						
int	tag,						
MPI_Comm	comm,						
MPI_Status	*status						

)



```
if (ID == j) {
    ...
   Receive from I
   ...
if (ID == i) {
   ...
   Send to j
   ...
```

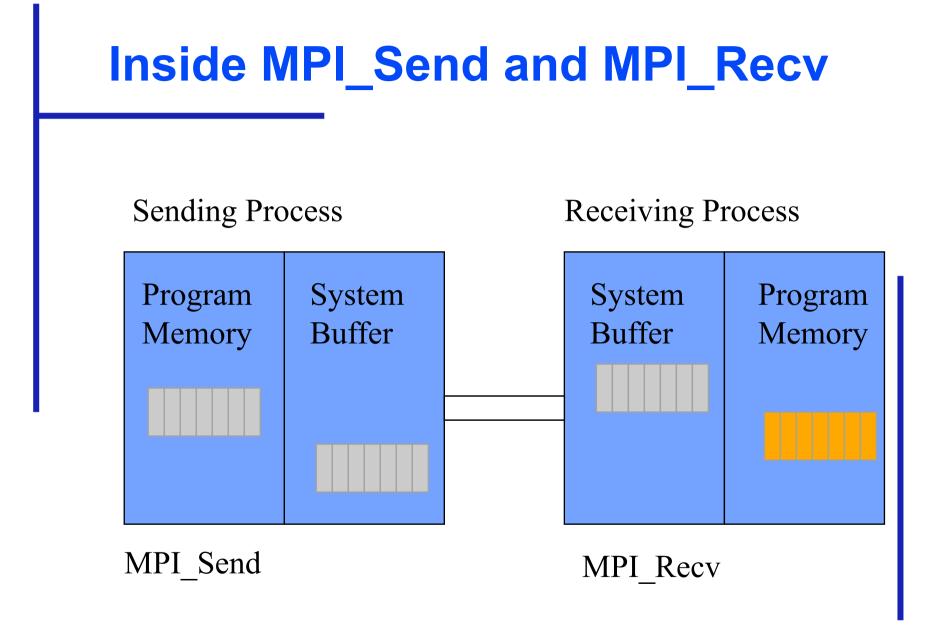
...

...

Receive is before Send. Why does this work?

variantes de send

 http://www.mcs.anl.gov/research/projects/mpi /sendmode.html

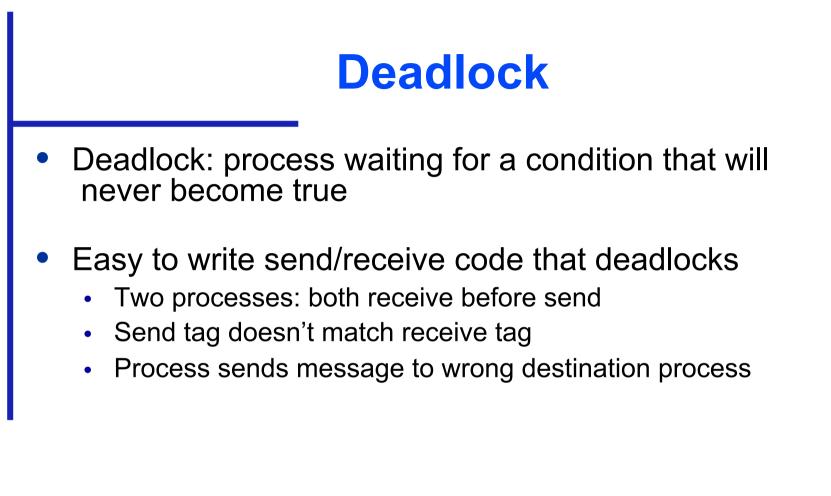


Return from MPI_Send

- Function blocks until message buffer free
- Message buffer is free when
 - Message copied to system buffer, or
 - Message transmitted
- Typical scenario
 - Message copied to system buffer
 - Transmission overlaps computation

Return from MPI_Recv

- Function blocks until message in buffer
- If message never arrives, function never returns



Function MPI_Bcast

```
int MPI_Bcast (
```

void *buffer, /* Addr of 1st element */

MPI_Datatype datatype, /* Type of elements *

int root, /* ID of root process */

MPI Comm comm) /* Communicator */

MPI Bcast (&k, 1, MPI INT, 0, MPI COMM WORLD);

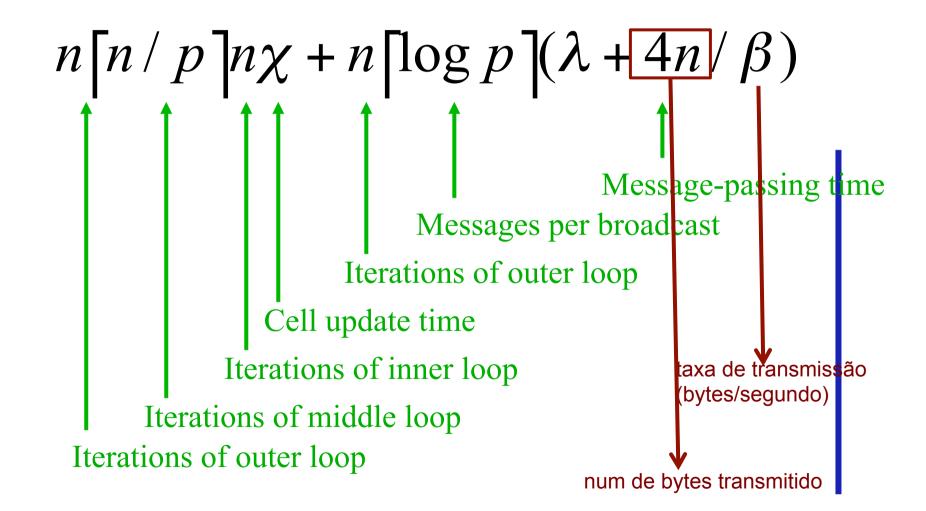
Computational Complexity

- Innermost loop has complexity $\Theta(n)$
- Middle loop executed at most [n/p] times
- Outer loop executed n times
- Overall complexity $\Theta(n^3/p)$

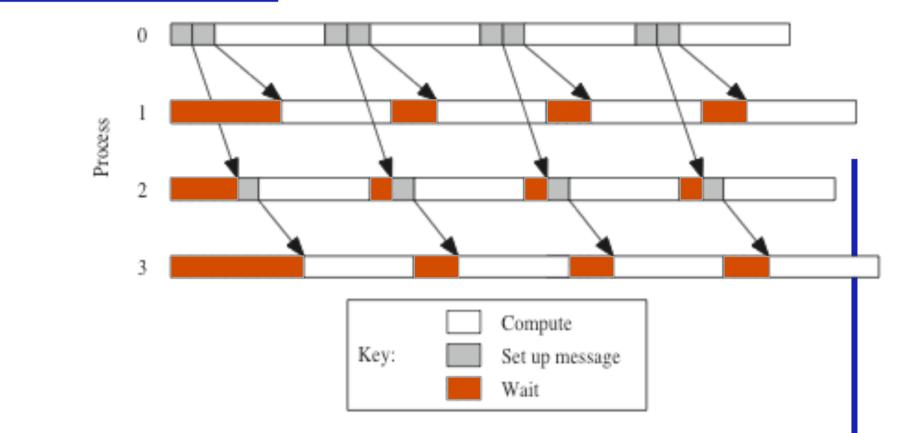
Communication Complexity

- No communication in inner loop
- No communication in middle loop
- Broadcast in outer loop complexity is $\Theta(n \log p)$
- Overall complexity $\Theta(n^2 \log p)$

Execution Time Expression (1)



Computation/communication Overlap



Execution Time Expression (2)

```
n \left[ n / p \right] n \chi + n \left[ \log p \right] \lambda + \left[ \log p \right] 4 n / \beta
                                              Message transmission
                                   Message-passing time
                               Messages per broadcast
                        Iterations of outer loop
                 Cell update time
             Iterations of inner loop
      Iterations of middle loop
Iterations of outer loop
```

Predicted vs. Actual Performance

	Execution Time (sec)	
Processes	Predicted	Actual
1	25.54	25.54
2	13.02	13.89
3	9.01	9.60
4	6.89	7.29
5	5.86	5.99
6	5.01	5.16
7	4.40	4.50
8	3.94	3.98



- Two matrix decompositions
 - Rowwise block striped
 - Columnwise block striped
- Blocking send/receive functions
 - MPI_Send
 - MPI_Recv
- Overlapping communications with computations